

# Theoretical Study of the Effect of Pressure on the Electronic Structure of Grey Tin

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**Abstract:** A large unit cell (LUC) within intermediate neglect of differential overlap (INDO) formalism has been used to estimate the electronic properties of  $\alpha$ -Sn and their pressure dependence. The calculated properties are, in general, in acceptable agreement with the available experimental values except the direct band gap. The calculated properties follow the usual qualitative trends that can be obtained from Hartree-Fock analysis. The increase of pressure is predicted to cause: a linear increase of the direct band gap with a pressure coefficient of 0.06 eV/GPa, a linear increase of the valence band width, a decrease of the conduction band width, a slight decrease of the electronic occupation probability for the s orbital with a slight increase of this probability for the p orbital, and a decrease of the X-ray scattering factors.

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## 1. INTRODUCTION

The electronic and structural properties of tin are very sensitive to pressure conditions [1]. The ground state, grey tin ( $\alpha$ -Sn), has the diamond structure and is known to be a semiconductor with zero band gap (semi-metal). Tin also exists in the  $\beta$ -Sn structure (white tin) at atmospheric pressure above 13°C. The metallic  $\beta$ -Sn phase is a tetragonal distortion of diamond with two atoms per unit cell. This phase is stable up to 9.5 GPa at room temperature, where it transforms to a bct form, followed by a transformation to the cubic bcc structure [2]. These temperature and pressure-driven phase transformations have caused tin to be of considerable experimental and theoretical interest [2-11].

The electronic and structural properties of complex systems like tin require a fully quantum-mechanical description. Accurate full first-principles calculations such as Hartree-Fock with correlation correction [12] and the local density approximation [13, 14] are extremely demanding from the computational point of view. The development of simpler yet reliable approximate methods of calculations is therefore crucial to progress in this field.

An alternative to first principle methods, which has already provided numerous significant results, is the so called the large unit cell-intermediate neglect of differential overlap (LUC-INDO) [15-18]. The semi-empirical LUC-INDO method is capable of simulating real crystals because it takes into account the property of periodicity. Due to its semi-empirical character and a specific parameterization

scheme, the computer program is not cumbersome and time consuming (about 1 hour for each process cycle) in the treatment of the electronic and spatial structure of simple systems as in our case. Also, it is suitable for analyzing complex systems [19-22].

A lot of studies have been carried out on the properties of tin and its phase transitions [1-11]. However, there are comparatively fewer studies on the pressure and temperature dependence of these properties. The aim of the present work is to investigate the effect of pressure on the electronic and structural properties of  $\alpha$ -Sn using the LUC-INDO formalism which will be outlined in the next section.

## 2. CALCULATION METHOD

A quantum-chemical semi-empirical INDO method developed especially for crystals [23] is used in the present work. This quantum computational formalism has been used with great success especially exploiting the so-called LUC (Large Unit Cell) model [18]. Within the method each molecular orbital is constructed as a linear combination of atomic orbitals [23] in order to express the wave function of the system. Each energy value is calculated by the HF self-consistent field method and the total energy of the system is obtained. The basic idea of LUC is in computing the electronic structure of the unit cell extended in a special manner at  $k=0$  in the reduced Brillouin zone. This equivalent to a band structure calculation at those  $k$  points; which transform to the Brillouin zone center on extending the unit cell [18].

The crystal wave function in the LUC-INDO formalism is written in the following form:

$$\psi_{(k,r)} = N_L^{-1/2} \sum_v \sum_p C_p(k) \phi_p(r - T_v) \exp(ik \cdot T_v) \quad (1)$$

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where  $N_L$  is the number of LUCs in the crystal,  $C_p(\mathbf{k})$  denotes the combination coefficients of the hybridized orbitals,  $\varphi$  is the atomic wave function,  $\mathbf{k}$  is the wave vector, and  $\mathbf{T}_v$  denotes the lattice translation vector. The Hartree-Fock equation in this case ( Roothaan-Hall equation ) can be written as [24]:

$$\sum_p (F_{pq}(\mathbf{k}) - \varepsilon(\mathbf{k}) S_{pq}(\mathbf{k})) C_p(\mathbf{k}) = 0 \quad (2)$$

where the summation index  $p$  goes over all the atomic states of the LUC,  $F_{pq}(\mathbf{k})$  represents the Fock Hamiltonian which is given by

$$F_{pq}(\mathbf{k}) = \sum_v \langle \varphi_p(\mathbf{r} - \mathbf{T}_o) | H^T | \varphi_q(\mathbf{r} - \mathbf{T}_v) \rangle \exp(i\mathbf{k} \cdot \mathbf{T}_v) \quad (3)$$

and  $S_{pq}(\mathbf{k})$  is the overlap integral defined by

$$S_{pq}(\mathbf{k}) = \sum_v \langle \varphi_p(\mathbf{r} - \mathbf{T}_o) | \varphi_q(\mathbf{r} - \mathbf{T}_v) \rangle \exp(i\mathbf{k} \cdot \mathbf{T}_v) \quad (4)$$

where  $H^T$  in Eq.(3) represents the Hamiltonian operator of the total energy  $E^T$  which is defined as

$$E^T = \sum_A \sum_{B < A} \frac{Z_A Z_B}{R_{AB}} + \frac{1}{2} \sum_{\mu} \sum_{\nu} P_{\lambda\sigma} (F_{\mu\nu} + H_{\mu\nu}^{core}) \quad (5)$$

where the first term of the right side of Eq.(5) represents the inter-nuclear potential energy, and  $P_{\lambda\sigma}$  is the density matrix which has the following expression:

$$P_{\lambda\sigma} = 2 \sum_{i,k}^{occ} C_{\lambda i}^*(\mathbf{k}) C_{\sigma i}(\mathbf{k}) \exp(i\mathbf{k} \cdot (\mathbf{T}_v - \mathbf{T}_\sigma)) \quad (6)$$

The summation is over the occupied (*occ*) orbitals only.  $H_{\mu\nu}^{core}$  refers to the matrix element of the Hamiltonian of a single electron in the field of the nuclei, and its operator representation is

$$H^{core} = -\frac{1}{2} \nabla^2 - \sum_A \frac{Z_A}{r} \quad (7)$$

where  $Z_A$  is the core charge, and the summation is over all nuclei. It should be pointed out that our calculations are carried out at  $\mathbf{k}=0$ , so  $\mathbf{k}$  value in eqs.(1,3,4,6) is set to zero. For more details of LUC-INDO formalism and the final form of the Fock matrix elements at  $\mathbf{k}=0$ , see Refs [15-18, 23-26]. The Roothaan-Hall equation are solved by first assuming an initial set of the linear expansion coefficient ( $C_p(\mathbf{k})$ ), generating the density matrix ( $P_{\lambda\sigma}$ ), and computing the overlap integral and the first guess of the Fock matrix elements ( $F_{pq}(\mathbf{k})$ ). Then one can calculate the electronic energy ( $E_e$ ), and a new matrix of  $C_p(\mathbf{k})$  coefficients can be obtained. This procedure is continued until there is no significant variation between the calculated value of  $C_p(\mathbf{k})$  and  $E$  of the successive iterations.

An initial guess of the wave function is predicted using the basis set and adopting Slater-type orbitals [23]. The initial guess of the wave function is important since an optimum guess reduces the number of iterations performed

to obtain the converged electronic energy. A large number of iterations will result in an accumulation of the computational errors. The  $sp^3$  initial guess of the wave function is given as an expected linear combination of the atomic states of one cell. The tolerance of convergence of the total electronic energy adopted in our calculations is  $10^{-8}$  eV. A large unit cell of 8 atoms, which is the conventional Bravais lattice of the diamond structure, has been used. Interactions of the atoms in the central Bravais lattice with the surrounding atoms up to the fourth neighbors are included. It should be pointed out that the increase of the LUC size will result in an increase of the results accuracy [27], but this complicates the calculations and needs very long time in comparison with the time needed for 8-atom LUC calculations.

### 3. RESULTS AND DISCUSSION

#### 3.1. Choice of Empirical Parameters

The empirical parameters included in the LUC-INDO method are the orbital exponent  $\zeta$ , the bonding parameter  $\beta^0$ ,  $\frac{1}{2}(I_s + A_s)$ , and  $\frac{1}{2}(I_p + A_p)$ . The symbols I and A refer to the ionization potential and the electron affinity respectively. The optimum values of these empirical parameters used for  $\alpha$ -Sn in the present work are listed in Table 1. The value of the orbital exponent  $\zeta$  determines the charge distribution of electrons around the nucleus. This parameter is varied till the total energy reaches its minimum value. As a consequence, this parameters is chosen in the same way of the ab initio methods. Comparing the  $\zeta$  value for  $\alpha$ -Sn crystal with that obtained by Clementi and Roetti ( $1.89 \text{ a.u}^{-1}$ ) [28] for atoms, shows that the  $\zeta$  value for solids is larger than that for atoms. This indicates the contracted charge distribution for solids and the diffuse charge distribution for atoms. The absolute value of the bonding parameter  $\beta^0$  of  $\alpha$ -Sn crystal is noted to be much smaller than that for molecules ( $-11.85 \text{ eV}$ ) [29]. This can be explained by noting that the number of bonds in solid is higher, then the interaction energy is distributed over all these bonds. The value of the  $\frac{1}{2}(I_s + A_s)$  parameter of  $\alpha$ -Sn crystal is less than the corresponding value of the tin free atom. This indicates that the s orbitals of the solid are less connected to their atoms than in the free atom. A reverse observation is reported for the  $\frac{1}{2}(I_p + A_p)$  parameter.

#### 3.2. Electronic and Structural Properties

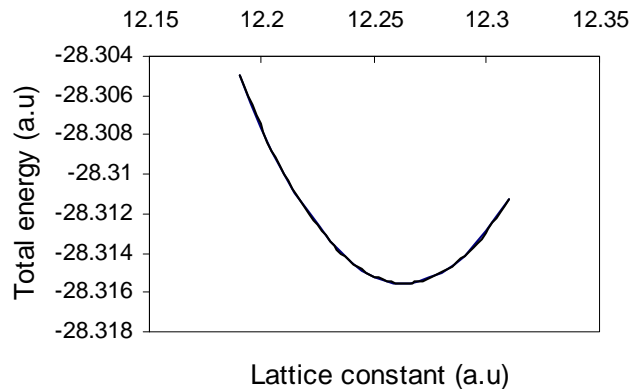
Using the computational procedure described in section 2, the electronic and structural properties of  $\alpha$ -Sn crystal at 0 K and zero pressure are calculated as listed in Table 2 in comparison with other computational and experimental results.

The equilibrium lattice constant ( $a_0$ ) is determined by plotting the total energy as a function of the lattice parameter, as depicted in Fig. (1). The calculated value of the

equilibrium lattice constant (12.263 a.u) is in good agreement with the estimated value of 12.184 a.u from the experimental data [30].

**Table 1. Empirical Parameters Used in the Present Work for  $\alpha - \text{Sn}$**

Parameter	Value
$\zeta(\text{a.u}^{-1})$	1.9965
$\beta^0(\text{eV})$	-5.3345
$\frac{1}{2}(I_s + A_s)(\text{eV})$	-9.452
$\frac{1}{2}(I_p + A_p)(\text{eV})$	-5.632



**Fig. (1).** Total energy of ( $\alpha - \text{Sn}$ ) as a function of lattice constant.

The cohesive energy is calculated from the total energy of the large unit cell. Since the large unit cell in the present work is composed of 8 atoms, the cohesive energy can be determined from the following expression:

$$E_{coh} = E^T / 8 - E_{free} - E_0 \quad (8)$$

where  $E_{free}$  denotes the free atom sp shell energy,  $E_0$  is the vibrational energy state, which is referred to as zero-point

energy, and its value is 0.03 eV [32]. The cohesive energy value of present work (-3.144 eV) is also in good agreement with the experimental value of -3.14 eV [31]. This is due to the including of the exchange integrals, correlation correction, and zero-point energy in the present analysis. The correlation correction is the correction included to take into account the fact that the motions of electrons are correlated pairwise to keep electrons apart. Correlation energies may be included by considering Slater determinants composed of orbitals that represent excited state contribution, and this method of including unoccupied orbitals in the many body wavefunction is referred to as configuration interaction (CI) [24]. Another method to estimate the correlation correction, which is used in the present work, is the Moller-Plesset perturbation theory [24]. This correction is calculated to be 0.27 eV. A detailed description of the several kinds of correlation corrections is present in reference [24].

The calculated direct band gap is considerably larger than the experimental value. A similar anomaly was also obtained by Svane [5] using the Hartree-Fock approximation. The large computed value of the direct band gap can be attributed to the approximations involved in the LUC-INDO formalism and Hartree-Fock method, and to the perturbative treatment of the correlation correction [33]. However, the available non-perturbative correlation correction method takes nearly ten times the computational time needed in Moller-Plesset method. The most significant approximations that affect the band gap are:

- (i). Using equal values of  $\zeta$  and  $\beta^0$  for s and p wavefunctions. The difference between bonding and anti-bonding states is directly proportional to  $\beta^0 S$ , where the overlap integral  $S$  is a function of  $\zeta$ . The percentage different of  $\zeta$  between s and p orbitals was reported to be 14.4% for tin [28].
- (ii). Neglecting the core states will also result in a neglect of its effects on the distribution of the outer valence electrons.
- (iii). Using the 5s 5p orbitals only without the inclusion of the 4d orbital.

**Table 2. The Electronic and Structural Properties of  $\alpha - \text{Sn}$  Crystal Obtained in the Present Work in Comparison with Other Results**

Property	Computational		Experimental Value
	Present Work	Others	
Lattice constant (a.u)	12.263	12.24 [2] 12.216 [1]	12.255 [30] (at R.T) 12.184 (at 0 K)
Cohesive energy (eV/atom)	-3.144	-2.8 [5] -3.723 [1]	-3.14 [27]
Valence band width (eV)	11.87	10.6 [5]	-----
Direct band gap (eV)	1.76	2.6 [5]	0.0 [31]
Conduction band width (eV)	5.2	-----	-----
Hybridization state	$s^{1.37} p^{2.63}$	-----	----

It should be pointed out that the present value for the band gap is a non-relativistic value. The computed band gap value of tin is expected to be in good agreement with the corresponding experimental value if the relativistic splitting of the levels [5] is considered, and if greater size of LUC is used [34], in addition to the points mentioned above.

The eigenvalues of the high symmetry points used to determine the band structure are listed in Table 3, in comparison with the corresponding values calculated by Svane [5].

**Table 3. Energy Bands of  $\alpha$  – Sn at  $\Gamma$  and X High Symmetry Points**

Symmetry Point	Eigenvalue (eV)	
	Present Work	Ref. [5]
$\Gamma_1$	-12.04	-16.0
$X_{1v}$	-7.08	-11.2
$X_{4v}$	-2.8	-3.9
$\Gamma_{25}$	0.0	0.0
$\Gamma_2$	1.5	2.6
$X_{1c}$	4.37	4.39
$X_{4c}$	6.92	-
$\Gamma_{15}$	5.19	6.6

Some physical properties of solids can be determined using the analysis described in the preceding section, such as the electronic charge density and the X-ray scattering factor, the valence electrons charge density ( $\rho_e(r)$ ) can be expressed as:

$$\rho(r) = \sum_p \sum_q P_{pq} \varphi_p(r) \varphi_q(r) \tag{9}$$

The electronic charge density for some planes of  $\alpha$ -Sn crystal is displayed in Fig. (2).

The X-ray scattering factor ( $f_j$ ) is defined by [31].

$$f_j = \int \rho_e(r) \exp(-iG.r) dV \tag{10}$$

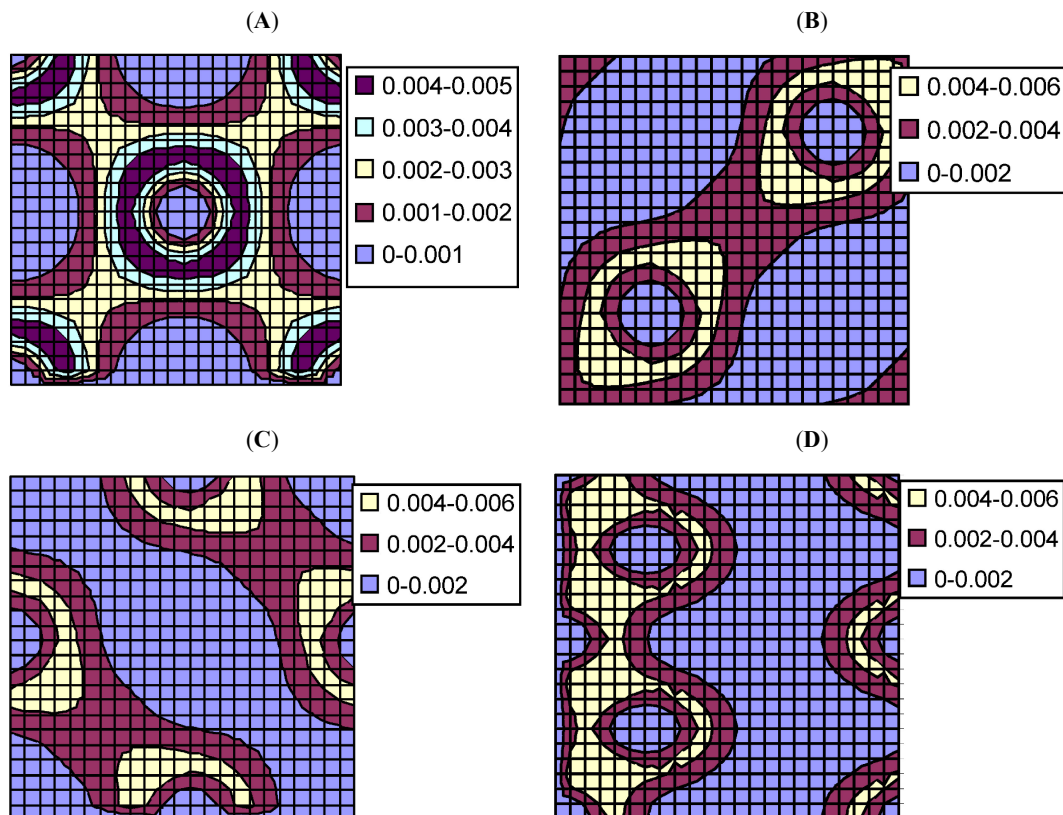
where  $G$  is the reciprocal lattice vector. In Table 4, the calculated X-ray scattering factors for  $\alpha$  – Sn are listed in comparison with other computational [35] and experimental [25] results. The calculated X-ray scattering factors are in good agreement with the experimental values.

### 3.3. Effect of pressure on the properties of $\alpha$ – Sn

The pressure dependence of the electronic structure can be predicted from the present computational analysis. The pressure dependence of the lattice parameter is determined using the Murnaghan [36] equation of state:

$$a = a_0 \left( 1 + \bar{B} \frac{P}{B_0} \right)^{-\frac{1}{3\bar{B}}} \tag{11}$$

where  $a$  is the lattice parameter at pressure  $P$ ,  $a_0$  is the

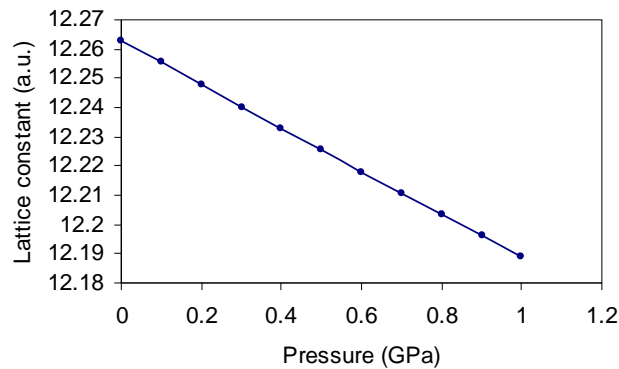


**Fig. (2).** Valence charge density (in atomic unit) of  $\alpha$  – Sn in the: (A) (001) plane, (B) (400) plane, (C) (200) plane, and (D) (110) plane.

lattice constant at zero pressure,  $B_0$  is the bulk modulus at zero pressure, and  $\bar{B}$  represents the pressure derivative of the bulk modulus and its value for  $\alpha$ -Sn is 4.6 [37]. The variation of the lattice parameter as a function of pressure for  $\alpha$ -Sn is depicted in Fig. (3). This figure was plotted using the experimental value of  $B_0$  of 53 GPa [38] and the calculated value of  $\bar{B}$  of 4.6 [37].

**Table 4. Calculated X-Ray Scattering Factors of  $\alpha$ -Sn Compared with Other Results**

$(hkl)$	X-Ray Scattering Factor		
	Present Work	HF [35]	Experimental [25]
(111)	44.45	44.47	43.59
(220)	39.57	39.56	38.79
(311)	37.44	37.43	37.40
(400)	35.37	34.54	35.12
(331)	33.03	33.08	33.17
(422)	30.63	31.01	30.19
(511)	30.34	29.93	28.63
(333)	29.42	29.93	28.63

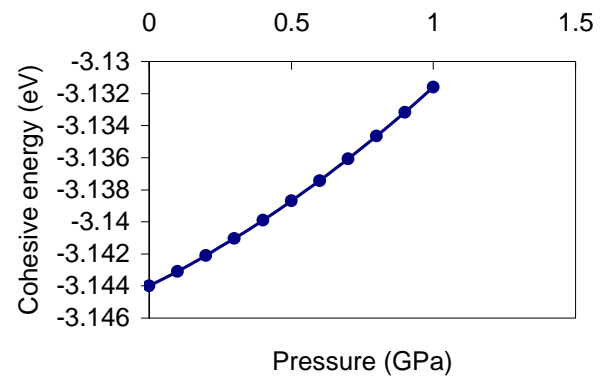


**Fig. (3).** Lattice constant of ( $\alpha$ -Sn) as a function of pressure.

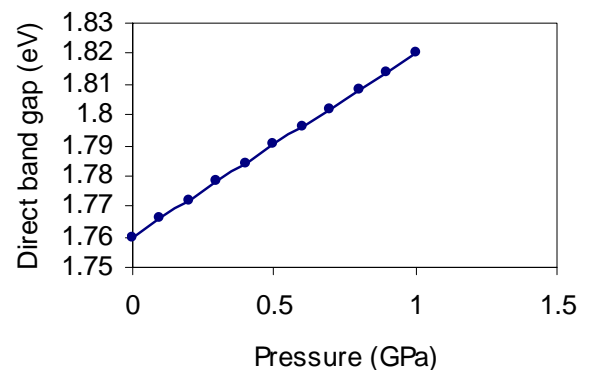
The pressure dependence of the cohesive energy, direct band gap, valence band width, and conduction band width as predicted from our analysis is shown in Figs. (4-7) respectively.

As it is obvious from Fig. (5), the direct band gap increases nearly linearly with the increase of the pressure. We suppose that this is mainly due to the nearly linear dependence of the lattice constant with the pressure as shown in Fig. (3), and since the translation vector ( $T_v$ ) scales linearly with the lattice constant, one can expect a nearly linear relation between the band gap and the pressure according to the present model. The pressure derivative of the direct band gap equals 0.06 eV/GPa. Wei and Zunger [37] have determined the pressure derivative of the band gap of the three main transitions;  $\Gamma$ -X,  $\Gamma$ -L, and  $\Gamma$ - $\Gamma$  for  $\alpha$ -Sn to be -0.01, 0.059, and 0.166 eV/GPa respectively. The direct band gap is determined from the energy

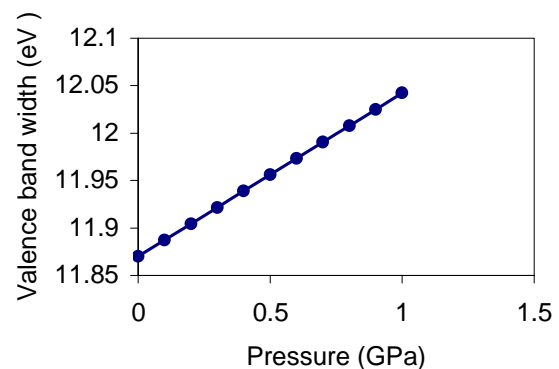
difference ( $\Gamma_2 - \Gamma_{25}$ ). The observed linear increase of the direct band gap with pressure is due to the linear increase of the  $\Gamma_2$  energy with respect to the  $\Gamma_{25}$  energy as found from the present analysis, and also by Bassani and Liu [3]. The valence band width is calculated from the energy difference ( $\Gamma_{25} - \Gamma_1$ ). The  $\Gamma_1$  state is shown to decrease linearly with the increase of pressure, and this causes a linear increase of the valence band width as depicted in Fig. (6). The conduction band width can be determined from the energy difference ( $X_{4C} - \Gamma_2$ ). Although the  $X_{4C}$  energy is shown to increase with pressure, the conduction band width decreases with pressure as shown in Fig. (7) because the increase of  $\Gamma_2$  energy is more than the increase of  $X_{4C}$  energy.



**Fig. (4).** Effect of pressure on the cohesive energy of grey tin.



**Fig. (5).** Effect of pressure on the direct band gap width of grey tin.



**Fig. (6).** Effect of pressure on the valence band width of grey tin.

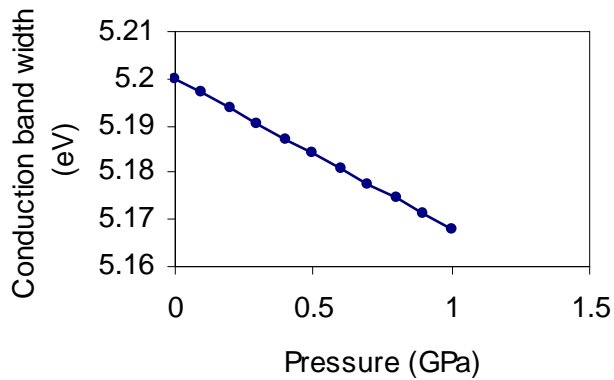


Fig. (7). Effect of pressure on the conduction band width of grey tin.

It is found that the s state occupation decreases with the increase of pressure as in Fig. (8), whereas the p state occupation increases with the increase of pressure as in Fig. (9).

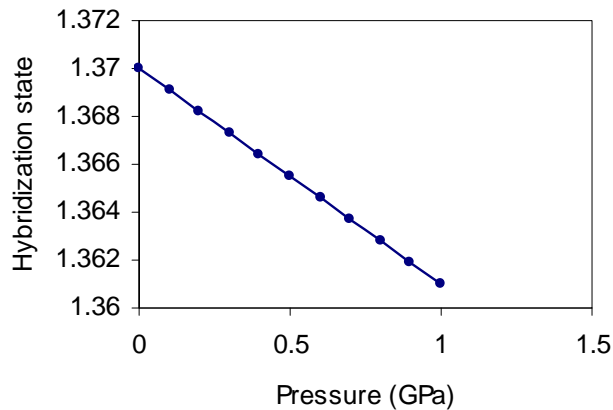


Fig. (8). Effect of pressure on the hybridization state of the s orbital of grey tin.

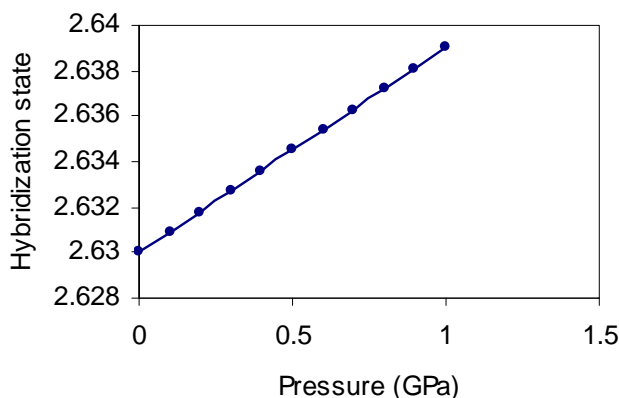


Fig. (9). Effect of pressure on the hybridization state of the p orbital of grey tin.

The present works shows that the X-ray scattering factors decrease as pressure increases. This behavior is obvious in Table 5. This can be interpreted as follows: increasing pressure decreases the inter-planer distance ( $d_{hkl}$ ), this increases the Bragg scattering angle (Bragg's law), and this in turn causes a decrease of the scattering wave intensity.

Table 5. Effect of Pressure on the X-Ray Scattering Factors of  $\alpha$ -Sn

(hkl)	X-Ray Scattering Factor at a Pressure of				
	0.2 (GPa)	0.4 (GPa)	0.6 (GPa)	0.8 (GPa)	1.0 (GPa)
(111)	44.447	44.437	44.427	44.417	44.407
(220)	39.562	39.547	39.532	39.518	39.503
(311)	37.426	37.410	37.393	37.376	37.360
(400)	35.353	35.335	35.317	35.298	35.280
(331)	33.009	32.988	32.966	32.944	32.923
(422)	30.611	30.586	30.561	30.537	30.512
(511)	30.318	30.295	30.271	30.248	30.224
(333)	29.398	29.373	29.348	29.323	29.298

#### 4. CONCLUSIONS

The present work shows that the semi-empirical LUC-INDO model can be used to simulate solids in a practical manner, because it is reasonably economical to use. The success of the approach depends on the optimum choice of the empirical parameter set and on the size of the LUC. Increasing the LUC size is expected to improve the result accuracy and reliability as it was confirmed by Harker and Larkins [27], but the increase of the LUC size results in a significant increase of the processing time. The calculated properties of  $\alpha$ -Sn are, in general, in acceptable agreement with the available experimental values, except the direct band gap. Increasing pressure is predicted to cause the following effects; a decrease of the absolute value of the cohesive energy, a linear increase of the direct band gap with a pressure coefficient of 0.06 eV/GPa, a linear increase of the valence band width, a decrease of the conduction band width, a slight decrease of the electronic occupation probability for the s orbital with a slight increase of this probability for the p orbital, and a decrease of the X-ray scattering factors. The above results show the usual trends that can be obtained from Hartree-Fock analysis which are a high band gap and acceptable qualitative results.

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#### REFERENCES

- [1] Aguado A. First-principles study of elastic properties and pressure-induced phase transitions of Sn: LDA versus GGA results. Phys Rev B 2003; 67: 212104-7.
- [2] Akdim B, Papaconstantopoulos DA, Mehl MJ. Tight-binding description of the electronic structure and total energy of tin. Philosophical Mag B 2002; 82: 47-61.
- [3] Bassani F, Liu L. Electronic band structure of gray tin. Phys Rev 1963; 132: 2047-50.
- [4] Pollak FH, Cardona M, Higginbotham CW, Herman F, Van Dyke JP. Energy-band structure and optical spectrum of grey tin. Phys Rev B 1970; 2: 352-63.

- [5] Svane A. Hartree-Fock band-structure calculations with the linear muffin-tin-orbital method: Application to C, Si, Ge, and  $\alpha$ -Sn. *Phys Rev B* 1987; 35: 5496-502.
- [6] Van Camp PE, Van Doren VE, Devreese JT. Ground-state and electronic properties of covalent solids. *Phys Rev B* 1988; 38: 12675-8.
- [7] Pavone P, Baroni S, de Gironcoli S.  $\alpha \leftrightarrow \beta$  phase transition in tin: a theoretical study based on density-functional perturbation theory. *Phys Rev B* 1998; 57: 10421-3.
- [8] Pavone P. Old and new aspects in lattice-dynamical theory. *J Phys: Condens Matter* 2001; 13: 7593-610.
- [9] Mujica A, Rubio A, Munoz A, Needs RJ. High-pressure phases of group-IV, III-V, and II-VI compounds. *Rev Mod Phys* 2003; 75: 863-912.
- [10] Bernard S, Maillet JB. First-principles calculation of the melting curve and Hugoniot of tin. *Phys Rev B* 2002; 66: 12103-6.
- [11] Katzke H, Bismayer U, Toledano P. Theory of the high-pressure structural phase transitions in Si, Ge, Sn, and Pb. *Phys Rev B* 2006; 73: 134105-14.
- [12] Ehrenreich H, Seitz F, Turnbull D, Eds. *Solid State Physics: Advances in Research and Applications*. New York: Academic Press 1980; vol. 35.
- [13] Matthew W, Foulks C, Haydock R. Tight-binding models and density-functional theory. *Phys Rev B* 1989; 39: 12520-39.
- [14] Garcia-Vidal FJ, Merino J, Perez R, Rincon R, Ortega J, Flores F. Density-functional approach to LCAO methods. *Phys Rev B* 1994; 50: 10537-47.
- [15] Evarestov R, Lovchikov V. Large unit cell calculations of solids in the CNDO approximation. *Phys Stat Sol (b)* 1997; 79: 743-51.
- [16] Harker AH, Larkins FP. A large unit cell semiempirical molecular orbital approach to the properties of solids. I. General theory. *J Phys C: Solid State Phys* 1979; 12: 2487-95.
- [17] Evarestov R, Smirnov V. Special points of the Brillouin zone and their use in the solid state theory. *Phys Stat Sol (b)* 1983; 119: 9-40.
- [18] Shluger AL, Stefanovich EV. Models of the self-trapped exciton and nearest-neighbor defect pair in  $\text{SiO}_2$ . *Phys Rev B* 1990; 42: 9664-73.
- [19] Eglitis RI, Christensen NE, Kotomin EA, Postnikov AV, Borstel G. First-principles and semiempirical calculations for  $F$  centers in  $\text{KNbO}_3$ . *Phys Rev B* 1997; 56: 8599-604.
- [20] Engel E, Schmidt K, Beljonne D, *et al.* Transient absorption spectroscopy and quantum-chemical studies of matrix-isolated perylene derivatives. *Phys Rev B* 2006; 73: 245216-24.
- [21] Barajas-Barraza RE, Guirado-López RA. Clustering of  $\text{H}_2$  molecules encapsulated in fullerene structures. *Phys Rev B* 2002; 66: 155426-37.
- [22] Ballo P, Harmatha LA. Cluster modified neglect of diatomic overlap parametrization of oxygen: study of oxygen defects in silicon. *Phys Rev B* 2003; 68: 153201-4.
- [23] Pople J, Beveridge D. *Approximate MO Theories*. New York: McGraw-Hill 1970.
- [24] Hehre W, Radom L, Schleyer P, Pople J. *Ab-initio molecular orbital theory*. New York: John Wiley and Sons 1986.
- [25] Abdulsattar MA. Self-consistent field calculations of covalent semiconductors. Ph. D. Thesis, University of Baghdad 1997.
- [26] Radi IO, Abdulsattar MA, Abdul-Lettif AM. Semiempirical LUC-INDO calculations on the effect of pressure on the electronic structure of diamond. *Phys Stat Sol B* 2007; 244 (4): 1304-17.
- [27] Harker AH, Larkins FP. A large unit cell semiempirical molecular orbital approach to the properties of solids. II. Covalent materials: diamond and silicon. *J Phys C: Solid State Phys* 1979; 12: 2497-508.
- [28] Clementi E, Roetti C. Roothaans-Hartree-Fock atomic wave functions: basis functions and their coefficients for ground and certain excited states of neutral and ionized atoms,  $z \leq 54$ . *Atom Data Nucl Data Tables* 1974; 14(3-4): 177-478.
- [29] Boca R. Inclusion of relativistic effects into ZDO methods. I. A quasi-relativistic CNDO/1. *Int J Quantum Chem* 1987; 31: 941-50.
- [30] Price DL, Rowe JM. The crystal dynamics of grey ( $\alpha$ ) tin at 90°K. *Solid State Commun* 1969; 7: 1433-8.
- [31] Kittel C. *Introduction to Solid State Physics*, 7th ed. New York: John Wiley Sons 1996.
- [32] Lambrecht W, Anderson O. Minimal basis sets in the linear muffin-tin orbital method: Application to the diamond-structure crystals C, Si, and Ge. *Phys Rev B* 1986; 34: 2439-49.
- [33] Yin M, Cohn M. Theory of static structural properties, crystal stability, and phase transformations: Application to Si and Ge. *Phys Rev B* 1982; 26: 5668-87.
- [34] Abdulsattar MA, Al-Bayati KH. Corrections and parametrization of semiempirical large unit cell method for covalent semiconductors. *Phys Rev B* 2007; 75: 245201-9.
- [35] Cromer D, Mann J. X-ray scattering factors computed from numerical Hartree-Fock wave functions. *Acta Cryst A* 1968; 24: 321-4.
- [36] Murnaghan FD. The compressibility of media under extreme pressures. *Proc Natl Acad Sci USA* 1944; 3: 244-7.
- [37] Wei SH, Zunger A. Predicted band-gap pressure coefficients of all diamond and zinc-blende semiconductors: chemical trends. *Phys Rev B* 1999; 60: 5404-11.
- [38] Buchenau CJ, Cardona M, Pollak FH. Raman scattering in gray tin. *Phys Rev B* 1971; 3: 1243-4.

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